

Multiplying Powers

(same base)

Rule:

For all numbers x and all integers m and n ,

$$x^m \cdot x^n = x^{m+n}$$



"This simply means ... when you are multiplying, and the bases are the same, you **ADD** the exponents."

Consider:

$$\begin{aligned}x^2 \cdot x^3 &= (x \cdot x) \cdot (x \cdot x \cdot x) \\ &= x \cdot x \cdot x \cdot x \cdot x \\ &= x^5\end{aligned}$$

...when in doubt, expand terms to see what is happening.

Observe this rule at work in the following examples:

1. $2^4(2^5)(2^2) = 2^{11}$

The bases are the same (all 2's), so the exponents are added.

2. $7b^2 \cdot b^5 = 7b^7$

The bases are the same, so the exponents are

added. Notice how the numbers in front of the bases (7 and 1) are being multiplied.

$$3. \quad a^2(a^3)(a^3) = a^8$$

The bases are the same (all a's), so the exponents are added.

$$4. \quad x^3(x^{-2})(x^4) = x^{3+(-2)+4} = x^5$$

The bases are the same (all x's), so the exponents are added.

Be careful when adding the **negative exponent**.

$$5. \quad 6a^3 \cdot 5a^4 = 30a^7$$

The bases are the same, so the exponents are added. The numbers in front of the bases are multiplied.

$$6. \quad -2s^3t^2(5s^4)(7t) = -70s^7t^3$$

The exponents are added for the bases that are the SAME. The numbers in front, the coefficients, are multiplied. Don't forget powers of 1, such as the power associated with t .

$$7. \quad (6r^4s^2)(2r^2s) = 12r^6s^3$$

The exponents are added for the bases that are the SAME. The coefficients are multiplied.

$$8. \quad -9x(x^2 - 7x + 15) = \\ -9x^3 + 63x^2 - 135x$$

The $-9x$ is multiplied times EACH term inside the parentheses, adding the exponents as the multiplication occurs.

$$9. \quad ab(3a + 2b) = 3a^2b + 2ab^2$$

The ab is multiplied times EACH term inside the parentheses, adding the exponents of similar bases as this process occurs.

$$10. \quad x^2y(x^3 - y) = x^5y - x^2y^2$$

The x^2y is multiplied times EACH term inside the parentheses, adding the exponents of similar bases as this process occurs.

Take one more look at the distributive property at work with a set of parentheses, along with this new rule:

Use the distributive property to simplify:

$$\begin{aligned} &4x^2(2x^3 + 5) \\ &= 4x^2(2x^3) + 4x^2(5) \\ &= 8x^5 + 20x^2 \end{aligned}$$